

Identifying JeT Substructure with N -subJesseness

Cari Cesarotti

Department of Physics, Harvard University, Cambridge, MA, 02138

April 1, 2021

Abstract

We introduce a novel observable— N -subJesseness—with the purpose of identifying and characterizing JeT substructure. This observable is empirically derived from studying the ParTonic composition of high-quality JeTs. In this work we demonstrate not only the strong correlation between large N -subJesseness and SM JeTs, but also the potential for discriminating JeTs from various NP samples. We study how several substructure observables can be combined to improve the classification of diverse physics scenarios.

1 Introduction

Detection of new physics (NP) at the Large Hadron Collider (LHC) has proved elusive [1]. This does not necessarily imply that there is no remaining possibility for discovery at the LHC, but instead suggests that NP may be hiding in previously unexplored regimes of event topology. A robust approach to discovering new physics is therefore to design searches without strong model dependence, that are sensitive to only generic characteristics of NP models. A potentially lucrative and recently revisited highly clever strategy [2–4] is then to develop tools that measure event characteristics that are fundamentally distinct from the Standard Model (SM).

The event topology of Quantum Chromodynamics (QCD) at the collider scale is characterized by its small 't Hooft coupling, therefore we primarily observe two- or three-jet events. NP events may have similar or distinct substructure; we can conceive of scenarios with strongly coupled (large 't Hooft coupling) dynamics at TeV scales that don't form jets, or models with collimated cascades of complicated decays that produce similar radiation patterns. It is therefore imperative that we understand jet substructure to be able to discriminate SM jets from NP.

The goal of this letter is the same as the previously stated overarching goal towards discovering new phenomena at the LHC, but with a slightly different approach. Here, we aim to distinguish the work of Jesse Thaler (JeT), a Scientist at MIT (SM), from that of other phenomenologists of similar UV¹ completion. We will frequently use JeT to refer to both the person and his publications. This should be easy to understand, as many of us feel no separation between our work and our essence of being. For the remainder of this letter, we will refer to the work done by other physicists as Non-Jesse Publications (NP). Thus, as promised, we aim to distinguish SM JeT samples from NP. In order to do so, we introduce a new observable that can characterize the substructure of these samples and be used as an efficient discriminant: N -subJesseness.

The outline is as follows. We begin in Sec. 2 by defining N -subJesseness and the methodology necessary for its computation. We then discuss the results of applying N -subJesseness to discrimi-

¹UV is a common abbreviation for *university*, implying of course the PhD program, and more specifically the timing of said program.

nate between the samples in Sec. 3. In Sec. 4 we conclude, and discuss the future relevancy of this new observable.

2 Definitions and Methodology

N -subJenessness, which we write as τ_J , is constructed to probe lexical substructure of physics publications. This observable is empirical by nature, as it emerged from studying the substructure of JeTs.

As with any data-driven particle physics analysis, we first assemble a sample of the twenty highest quality—i.e. most citations—JeTs [5–24]. As a baseline, we also consider pure JeT samples, meaning single author JeTs [25,26]. We call these the multi JeT and single JeT samples respectively. Note that we remove community papers, as the true degree of JeT-iness is largely unknown.

The fundamental physics within each JeT is identified using the Python NLTK [27]. With this toolkit, we can cluster and enumerate the Parsed Tokens (ParTons), or words, in the JeT.

The extraction of JeT substructure information is nontrivial. Much like QCD jet events produced at the LHC, there is some due diligence required to reconstruct the underlying physics. The ParTons of a JeT do not appear in isolation; like quarks in protons, they obey the constraints of a PDF. To probe the substructure, we must be mindful of *hadronization*, or Having Difficulties Rendering ONline Information, reorganiZing arXiv-preprints as Text In Order to Numerate. The *hadronization* of JeTs potentially obfuscates some of the underlying physics of interest, but it does not substantially change the dominant substructure. Some soft ParTons may be lost or combined, but the overall analysis is robust.

After *hadronization*, the JeTs still contain auxiliary information such as symbols, equations, and generic non-ascii characters. We restrict our focus to only the highest frequency ParTons. In order to accurately understand its substructure, we must further refine the JeT and remove this lexical noise. We do so by *grooming*, or Getting Rid of Odd Misrepresentations of equatIons, Numbers, and Graphs. Once the JeTs have undergone *hadronization* and *grooming*, they are in a suitable format for us to begin the analysis.

We make several additional cuts at this stage to remove Irrelevant Reading (IR) divergences, as they have no observable affect on the phenomenology. For additional information on these cuts,

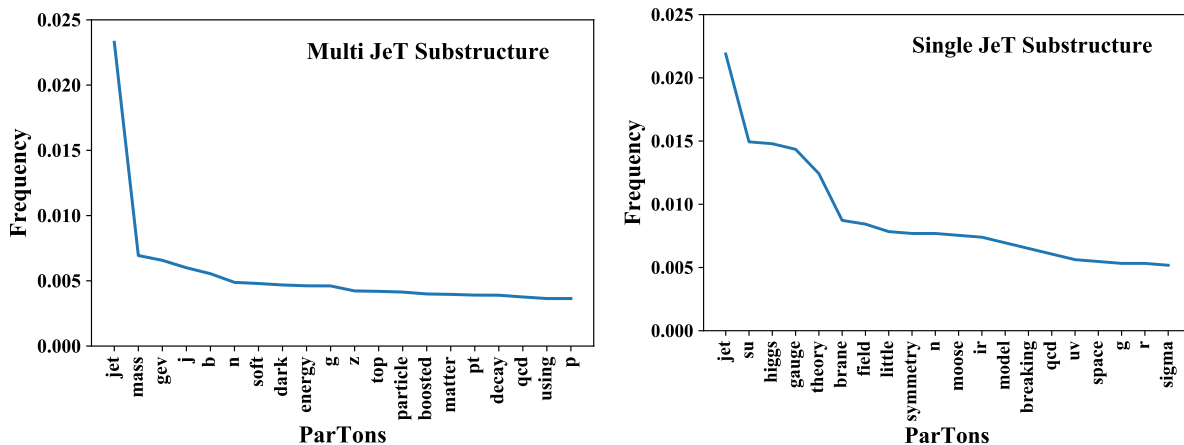


Figure 1: The relative ParTon abundance in the multi-JeT sample (left) and single-Jet sample (right). Note the obvious prevalence of *jet*.

see App. A. The output of the NLTK analysis is shown in Fig. 1.

The identifier of JeTs is clear: the high frequency of the word *jet* is a fundamental characteristic of a JeT. We therefore define N -subJenessness as

$$\tau_J \equiv \text{Freq}(jet). \quad (2.1)$$

In this letter we consider both local (per publication) as well as global (integrated over several highly-cited publications) N -subJenessness for characterization of these samples.

3 Results

Although the global τ_J of the JeT samples is striking, we cannot a priori claim that it is an efficient discriminator of SM JeT physics from NP. In this section, we first consider the substructure of various NP scenarios, and explore the discrimination efficiencies using τ_J and additional substructure observables. In all of our NP scenarios, we consider 10 high-quality samples again after *hadronization* and *grooming*.

An important NP scenario to consider is that of Arkani-Hamed [28–37]. Since the physics of this scenario had potentially strong influence on the formative stages of JeTs, it is important to compare the substructure of such physics. The ParTon distribution is shown in Fig. 2. Miraculously, even the global τ_J is exactly zero. This demands the question as to whether Arkani-Hamed was ever actually in causal contact with JeTs, but this fundamental concern is left to future work.

For other NP comparisons, we consider several scenarios constructed in the similar era. Namely, we consider Reece [38–47], Wang [7, 12, 39, 40, 48–53], Williams² [54–63], Slatyer [31, 64–72], Ruderman [43, 50, 53, 73–79], and Fan [39, 41–43, 46, 79–82] NP constructions. An overview of the global substructure is shown in Fig. 3. Note that while *jet* and its symbolic representation *j* occur in many of these scenarios, the relative abundance is still far below that of the multi JeT sample.

²This sample is equivalent to the LHCb NP scenario.

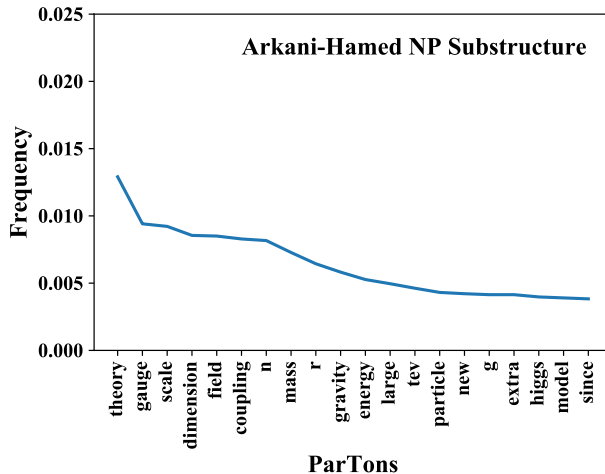


Figure 2: The relative ParTon abundance of Arkani-Hamed NP. Note that the global value of τ_J is exactly zero.

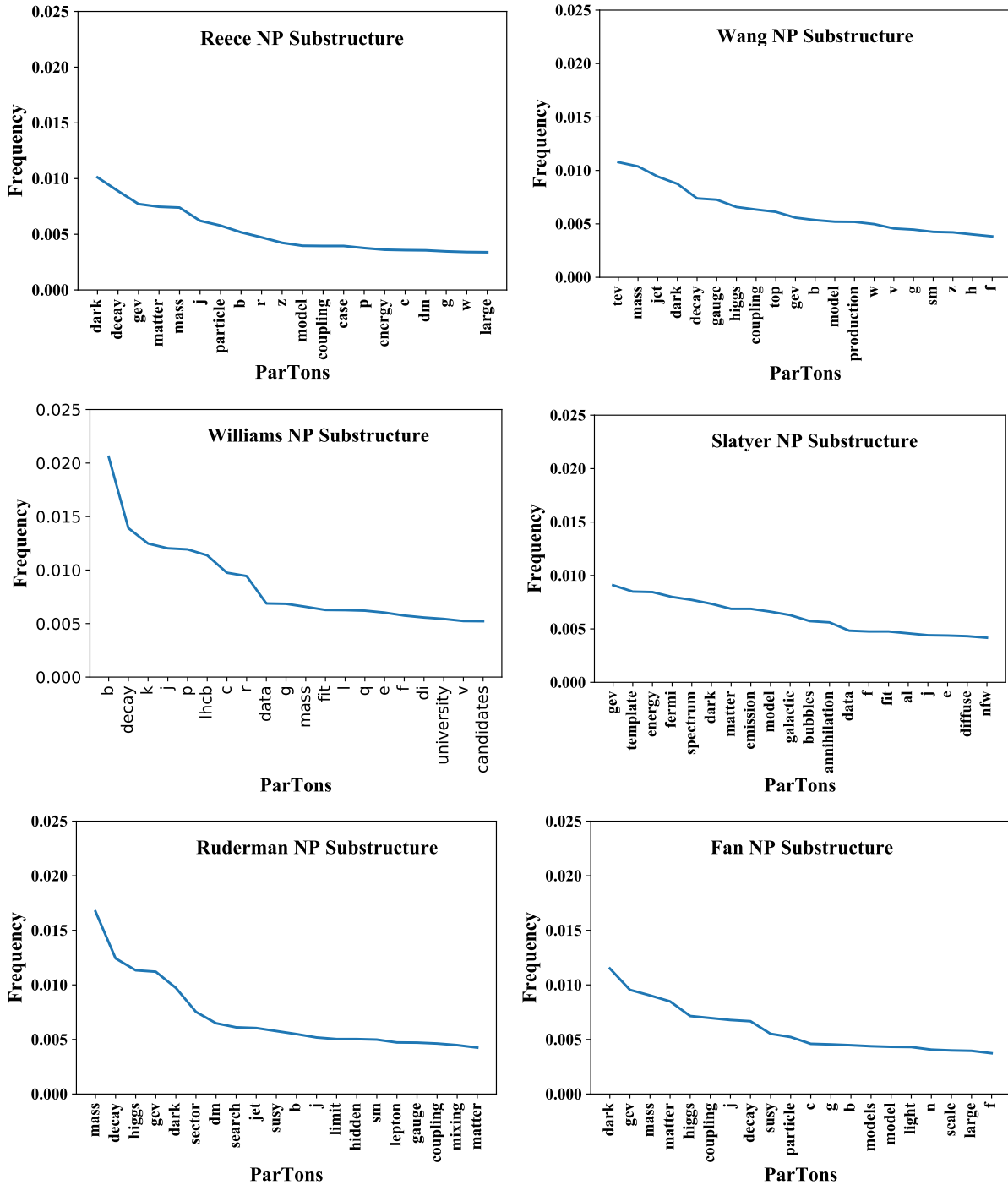


Figure 3: The relative ParTon abundance of various NP scenarios. There are several notable features of these distributions. For example, the Reece, Wang, Ruderman, and Fan scenarios all have very similar substructure. The Reece, Ruderman, and Fan samples are high in *gev*, whereas the Wang sample has a greater abundance of *tev*, suggesting that the Wang scenario can probe physics at larger energy scales. The only two scenarios that are concerned with data are the Slatyer and Williams NP, which begs the question of feasibility of the other scenarios. All scenarios have considerable abundances of *mass* and *decay*, confirming that particle physics research is being done at least at an undergraduate level.

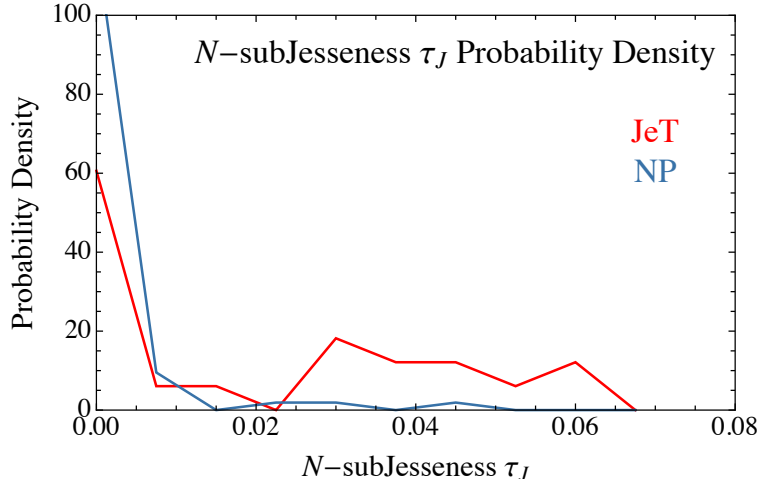


Figure 4: Probability density distribution in τ_J of the JeT (red) and NP (blue) samples.

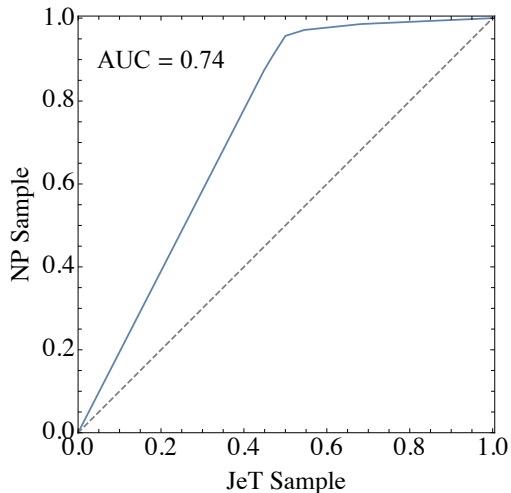


Figure 5: The ROC curve for discriminating the JeT sample from the NP sample. The AUC is 0.74, substantially better than naive random guessing.

3.1 The Discrimination Efficiency of N -subJenessess

We now aim to quantify how efficient τ_J is at discriminating between the JeT and NP scenarios. For higher statistics, we combine all of the mentioned NP samples into one larger sample, which we refer to holistically as NP. We also combine the single and multi JeT samples. The probability density in τ_J of these samples is shown in Fig. 4.

To quantify the separation of these distributions, we plot the approximate receiver operating characteristic (ROC) curve in Fig. 5 and integrate to attain the area under the curve (AUC). For reference, the worst case scenario of a constant slope ROC is drawn. This corresponds to an AUC of 0.5, which is realized for categorizing the samples by random guessing. When samples are perfectly separated, the AUC is 1.

We see that the the AUC is roughly 0.74, indicating improvement over random guessing. Therefore, even in this minimal inclusive analysis, we can use N -subJenessess as a means towards discriminating SM JeT and NP samples.

3.2 N -subJenessness and $decay$ Rates

In this section we explore the potential of characterizing JeT and NP scenarios in 2d parameter space: τ_J and $decay$ frequency, which we write as

$$\tau_{decay} \equiv \text{Freq}(decay). \tag{3.1}$$

We chose $decay$ as NP $decay$ can often introduce novel event topologies distinct from SM JeTs. This discussion is very brief, and is only meant to introduce the concept rather than fully exhaust its potential. We therefore consider the global τ_J and τ_{decay} . The distribution of JeT samples and NP scenarios is shown in Fig. 6.

We find that generically the JeT samples occupy a distinct region of parameter space from the NP scenarios, many of which are clustered together. This suggests that one could improve the separation between the JeT and NP samples by considering several other JeT substructure observables. This is an excellent proof of concept, and we encourage others in the community to pursue more in-depth analyses using this strategy.

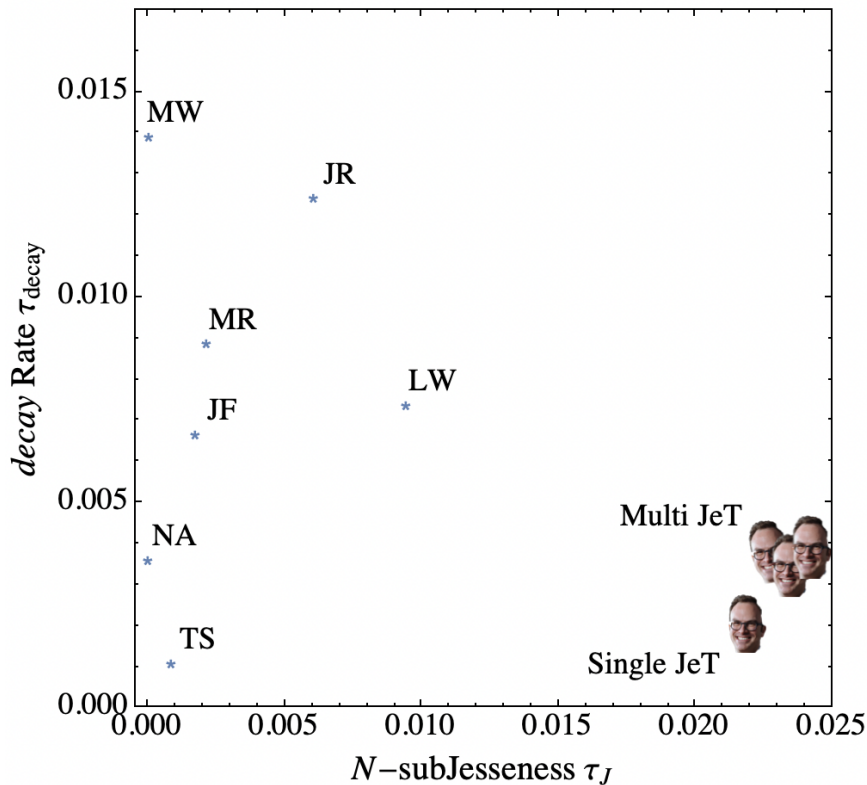


Figure 6: Distribution of JeT and NP samples in global τ_J - τ_{decay} 2d parameter space.

4 Discussion

Ultimately we have shown that N -subJenessness is an excellent identifier of SM JeTs. The substructure of a JeT is inherently much jettier than that of a generic NP scenario. This observable has strong potential to inform previous searches at the LHC, as well as hopefully future collider

analyses. We would be very interested to see an application of JeT at a possible future muon collider.

The discrimination power of τ_J alone was nontrivial, but there are certainly ways it can be improved. For instance, it is tempting to want to apply machine learning techniques to further optimize the efficiency of NP vs. JeT classification. However, we find the discrimination efficiency was not improved after employing multi-level neural networks and training for an appropriate amount of CPU hours. One maybe be able to construct a more sophisticated convolutional neural network or utilize Deep Learning to improve the efficiency, but the leading methodology remains anthropic³. From these results, we must pose the question to the field as to whether or not machine learning is the future of identifying JeT substructure or NP, as our studies are less than promising.

To conclude, we strongly suggest the use of N -subJeness whenever one needs to predict or understand the JeT content of a physics publication.

5 Acknowledgements

We would like to acknowledge Matthew Reece, Sam Homiller, Patrick Komiske, Rashmish Mishra, and Julián B. Muñoz for useful discussions. We would like to thank Zak Vendeiro in particular for his indispensable creative input. We would like to apologize to Nima Arkani-Hamed, Lian-Tao Wang, Mike Williams, Tracy Slatyer, Josh Ruderman, JiJi Fan, and of course Jesse Thaler, and hope that they have a good sense of humor. We do not feel the need to apologize to MR. CC is supported by various grants, but assures them that this was not done during the time for which they pay her.

A Further *Grooming*

In order to parse the samples in good faith, some additional grooming was needed. For example, trivial phrases that appear many times in all physics publications, such as `eq.`, `Sec.`, `JHEP`, etc. were removed as they occur with high frequency but do not contain any physics information.

Beyond these superfluous words, the issue of pluralization also required attention. Special care was taken to ensure that high-frequency words such as *theories*, *couplings*, *jets*, etc. were counted as their singular form. The NLTK offers a tool to automatically revert all words back to their stem, the `stemmer`, but this often over trimmed words and resulted in distributions in bizarre pseudo-words that offered much less comedic effect.

References

- [1] P. J. Fox, D. E. Kaplan, E. Katz, E. Poppitz, V. Sanz, M. Schmaltz, M. D. Schwartz, and N. Weiner, “Supersplit supersymmetry,” `arXiv:hep-th/0503249`.
- [2] C. Cesarotti and J. Thaler, “A Robust Measure of Event Isotropy at Colliders,” *JHEP* **08** (2020) 084, `arXiv:2004.06125` [`hep-ph`].
- [3] C. Cesarotti, M. Reece, and M. J. Strassler, “Spheres To Jets: Tuning Event Shapes with 5d Simplified Models,” `arXiv:2009.08981` [`hep-ph`].
- [4] C. Cesarotti, M. Reece, and M. J. Strassler, “The Efficacy of Event Isotropy as an Event Shape Observable,” `arXiv:2011.06599` [`hep-ph`].

³A more technical term for this process is known as *eyeballing*.

- [5] N. Arkani-Hamed, G. L. Kane, J. Thaler, and L.-T. Wang, “Supersymmetry and the LHC inverse problem,” *JHEP* **08** (2006) 070, [arXiv:hep-ph/0512190](#).
- [6] A. Pierce and J. Thaler, “Natural Dark Matter from an Unnatural Higgs Boson and New Colored Particles at the TeV Scale,” *JHEP* **08** (2007) 026, [arXiv:hep-ph/0703056](#).
- [7] J. Thaler and L.-T. Wang, “Strategies to Identify Boosted Tops,” *JHEP* **07** (2008) 092, [arXiv:0806.0023 \[hep-ph\]](#).
- [8] Y. Nomura and J. Thaler, “Dark Matter through the Axion Portal,” *Phys. Rev. D* **79** (2009) 075008, [arXiv:0810.5397 \[hep-ph\]](#).
- [9] J. Mardon, Y. Nomura, D. Stolarski, and J. Thaler, “Dark Matter Signals from Cascade Annihilations,” *JCAP* **05** (2009) 016, [arXiv:0901.2926 \[hep-ph\]](#).
- [10] D. Krohn, J. Thaler, and L.-T. Wang, “Jets with Variable R,” *JHEP* **06** (2009) 059, [arXiv:0903.0392 \[hep-ph\]](#).
- [11] M. Freytsis, G. Ovanesyan, and J. Thaler, “Dark Force Detection in Low Energy e-p Collisions,” *JHEP* **01** (2010) 111, [arXiv:0909.2862 \[hep-ph\]](#).
- [12] D. Krohn, J. Thaler, and L.-T. Wang, “Jet Trimming,” *JHEP* **02** (2010) 084, [arXiv:0912.1342 \[hep-ph\]](#).
- [13] F. D’Eramo and J. Thaler, “Semi-annihilation of Dark Matter,” *JHEP* **06** (2010) 109, [arXiv:1003.5912 \[hep-ph\]](#).
- [14] J. Thaler and K. Van Tilburg, “Identifying Boosted Objects with N-subjettiness,” *JHEP* **03** (2011) 015, [arXiv:1011.2268 \[hep-ph\]](#).
- [15] J. Thaler and K. Van Tilburg, “Maximizing Boosted Top Identification by Minimizing N-subjettiness,” *JHEP* **02** (2012) 093, [arXiv:1108.2701 \[hep-ph\]](#).
- [16] A. J. Larkoski, G. P. Salam, and J. Thaler, “Energy Correlation Functions for Jet Substructure,” *JHEP* **06** (2013) 108, [arXiv:1305.0007 \[hep-ph\]](#).
- [17] A. J. Larkoski, D. Neill, and J. Thaler, “Jet Shapes with the Broadening Axis,” *JHEP* **04** (2014) 017, [arXiv:1401.2158 \[hep-ph\]](#).
- [18] A. J. Larkoski, S. Marzani, G. Soyez, and J. Thaler, “Soft Drop,” *JHEP* **05** (2014) 146, [arXiv:1402.2657 \[hep-ph\]](#).
- [19] K. Agashe, Y. Cui, L. Necib, and J. Thaler, “(In)direct Detection of Boosted Dark Matter,” *JCAP* **10** (2014) 062, [arXiv:1405.7370 \[hep-ph\]](#).
- [20] A. J. Larkoski, J. Thaler, and W. J. Waalewijn, “Gaining (Mutual) Information about Quark/Gluon Discrimination,” *JHEP* **11** (2014) 129, [arXiv:1408.3122 \[hep-ph\]](#).
- [21] Y. Kahn, B. R. Safdi, and J. Thaler, “Broadband and Resonant Approaches to Axion Dark Matter Detection,” *Phys. Rev. Lett.* **117** no. 14, (2016) 141801, [arXiv:1602.01086 \[hep-ph\]](#).
- [22] P. Ilten, Y. Soreq, J. Thaler, M. Williams, and W. Xue, “Proposed Inclusive Dark Photon Search at LHCb,” *Phys. Rev. Lett.* **116** no. 25, (2016) 251803, [arXiv:1603.08926 \[hep-ph\]](#).

- [23] I. Moutl, L. Necib, and J. Thaler, “New Angles on Energy Correlation Functions,” *JHEP* **12** (2016) 153, [arXiv:1609.07483 \[hep-ph\]](#).
- [24] E. M. Metodiev, B. Nachman, and J. Thaler, “Classification without labels: Learning from mixed samples in high energy physics,” *JHEP* **10** (2017) 174, [arXiv:1708.02949 \[hep-ph\]](#).
- [25] J. Thaler, “Little technicolor,” *JHEP* **07** (2005) 024, [arXiv:hep-ph/0502175](#).
- [26] J. Thaler, “Jet maximization, axis minimization, and stable cone finding,” *Phys. Rev. D* **92** no. 7, (2015) 074001, [arXiv:1506.07876 \[hep-ph\]](#).
- [27] S. Bird, E. Loper, and E. Klein, *Natural Language Processing with Python*. O’Reilly Media Inc., 2009.
- [28] N. Arkani-Hamed, S. Dimopoulos, and G. R. Dvali, “The Hierarchy problem and new dimensions at a millimeter,” *Phys. Lett. B* **429** (1998) 263–272, [arXiv:hep-ph/9803315](#).
- [29] I. Antoniadis, N. Arkani-Hamed, S. Dimopoulos, and G. R. Dvali, “New dimensions at a millimeter to a Fermi and superstrings at a TeV,” *Phys. Lett. B* **436** (1998) 257–263, [arXiv:hep-ph/9804398](#).
- [30] N. Arkani-Hamed, S. Dimopoulos, and G. R. Dvali, “Phenomenology, astrophysics and cosmology of theories with submillimeter dimensions and TeV scale quantum gravity,” *Phys. Rev. D* **59** (1999) 086004, [arXiv:hep-ph/9807344](#).
- [31] N. Arkani-Hamed, D. P. Finkbeiner, T. R. Slatyer, and N. Weiner, “A Theory of Dark Matter,” *Phys. Rev. D* **79** (2009) 015014, [arXiv:0810.0713 \[hep-ph\]](#).
- [32] N. Arkani-Hamed, A. G. Cohen, and H. Georgi, “Electroweak symmetry breaking from dimensional deconstruction,” *Phys. Lett. B* **513** (2001) 232–240, [arXiv:hep-ph/0105239](#).
- [33] N. Arkani-Hamed, A. G. Cohen, E. Katz, and A. E. Nelson, “The Littlest Higgs,” *JHEP* **07** (2002) 034, [arXiv:hep-ph/0206021](#).
- [34] N. Arkani-Hamed and S. Dimopoulos, “Supersymmetric unification without low energy supersymmetry and signatures for fine-tuning at the LHC,” *JHEP* **06** (2005) 073, [arXiv:hep-th/0405159](#).
- [35] N. Arkani-Hamed, H.-C. Cheng, M. A. Luty, and S. Mukohyama, “Ghost condensation and a consistent infrared modification of gravity,” *JHEP* **05** (2004) 074, [arXiv:hep-th/0312099](#).
- [36] N. Arkani-Hamed, L. Motl, A. Nicolis, and C. Vafa, “The String landscape, black holes and gravity as the weakest force,” *JHEP* **06** (2007) 060, [arXiv:hep-th/0601001](#).
- [37] N. Arkani-Hamed and M. Schmaltz, “Hierarchies without symmetries from extra dimensions,” *Phys. Rev. D* **61** (2000) 033005, [arXiv:hep-ph/9903417](#).
- [38] P. Draper, P. Meade, M. Reece, and D. Shih, “Implications of a 125 GeV Higgs for the MSSM and Low-Scale SUSY Breaking,” *Phys. Rev. D* **85** (2012) 095007, [arXiv:1112.3068 \[hep-ph\]](#).
- [39] J. Fan, M. Reece, and L.-T. Wang, “Non-relativistic effective theory of dark matter direct detection,” *JCAP* **11** (2010) 042, [arXiv:1008.1591 \[hep-ph\]](#).

- [40] M. Reece and L.-T. Wang, “Searching for the light dark gauge boson in GeV-scale experiments,” *JHEP* **07** (2009) 051, arXiv:0904.1743 [hep-ph].
- [41] J. Fan and M. Reece, “In Wino Veritas? Indirect Searches Shed Light on Neutralino Dark Matter,” *JHEP* **10** (2013) 124, arXiv:1307.4400 [hep-ph].
- [42] J. Fan, A. Katz, L. Randall, and M. Reece, “Double-Disk Dark Matter,” *Phys. Dark Univ.* **2** (2013) 139–156, arXiv:1303.1521 [astro-ph.CO].
- [43] J. Fan, M. Reece, and J. T. Ruderman, “Stealth Supersymmetry,” *JHEP* **11** (2011) 012, arXiv:1105.5135 [hep-ph].
- [44] C. Csaki and M. Reece, “Toward a systematic holographic QCD: A Braneless approach,” *JHEP* **05** (2007) 062, arXiv:hep-ph/0608266.
- [45] Y. Kats, P. Meade, M. Reece, and D. Shih, “The Status of GMSB After 1/fb at the LHC,” *JHEP* **02** (2012) 115, arXiv:1110.6444 [hep-ph].
- [46] P. Agrawal, J. Fan, B. Heidenreich, M. Reece, and M. Strassler, “Experimental Considerations Motivated by the Diphoton Excess at the LHC,” *JHEP* **06** (2016) 082, arXiv:1512.05775 [hep-ph].
- [47] P. Meade and M. Reece, “BRIDGE: Branching ratio inquiry / decay generated events,” arXiv:hep-ph/0703031.
- [48] T. Han, H. E. Logan, B. McElrath, and L.-T. Wang, “Phenomenology of the little Higgs model,” *Phys. Rev. D* **67** (2003) 095004, arXiv:hep-ph/0301040.
- [49] B. Lillie, L. Randall, and L.-T. Wang, “The Bulk RS KK-gluon at the LHC,” *JHEP* **09** (2007) 074, arXiv:hep-ph/0701166.
- [50] M. Baumgart, C. Cheung, J. T. Ruderman, L.-T. Wang, and I. Yavin, “Non-Abelian Dark Sectors and Their Collider Signatures,” *JHEP* **04** (2009) 014, arXiv:0901.0283 [hep-ph].
- [51] A. L. Fitzpatrick, J. Kaplan, L. Randall, and L.-T. Wang, “Searching for the Kaluza-Klein Graviton in Bulk RS Models,” *JHEP* **09** (2007) 013, arXiv:hep-ph/0701150.
- [52] N. Arkani-Hamed, T. Han, M. Mangano, and L.-T. Wang, “Physics opportunities of a 100 TeV proton–proton collider,” *Phys. Rept.* **652** (2016) 1–49, arXiv:1511.06495 [hep-ph].
- [53] C. Cheung, J. T. Ruderman, L.-T. Wang, and I. Yavin, “Kinetic Mixing as the Origin of Light Dark Scales,” *Phys. Rev. D* **80** (2009) 035008, arXiv:0902.3246 [hep-ph].
- [54] **LHCb** Collaboration, R. Aaij *et al.*, “Observation of $J/\psi p$ Resonances Consistent with Pentaquark States in $\Lambda_b^0 \rightarrow J/\psi K^- p$ Decays,” *Phys. Rev. Lett.* **115** (2015) 072001, arXiv:1507.03414 [hep-ex].
- [55] **LHCb** Collaboration, R. Aaij *et al.*, “Test of lepton universality using $B^+ \rightarrow K^+ \ell^+ \ell^-$ decays,” *Phys. Rev. Lett.* **113** (2014) 151601, arXiv:1406.6482 [hep-ex].
- [56] **LHCb** Collaboration, R. Aaij *et al.*, “Measurement of the ratio of branching fractions $\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} \tau^- \bar{\nu}_\tau) / \mathcal{B}(\bar{B}^0 \rightarrow D^{*+} \mu^- \bar{\nu}_\mu)$,” *Phys. Rev. Lett.* **115** no. 11, (2015) 111803, arXiv:1506.08614 [hep-ex]. [Erratum: *Phys.Rev.Lett.* 115, 159901 (2015)].

- [57] **LHCb** Collaboration, R. Aaij *et al.*, “LHCb Detector Performance,” *Int. J. Mod. Phys. A* **30** no. 07, (2015) 1530022, [arXiv:1412.6352 \[hep-ex\]](#).
- [58] **LHCb** Collaboration, R. Aaij *et al.*, “Angular analysis of the $B^0 \rightarrow K^{*0}\mu^+\mu^-$ decay using 3 fb⁻¹ of integrated luminosity,” *JHEP* **02** (2016) 104, [arXiv:1512.04442 \[hep-ex\]](#).
- [59] **CMS, LHCb** Collaboration, V. Khachatryan *et al.*, “Observation of the rare $B_s^0 \rightarrow \mu^+\mu^-$ decay from the combined analysis of CMS and LHCb data,” *Nature* **522** (2015) 68–72, [arXiv:1411.4413 \[hep-ex\]](#).
- [60] **LHCb** Collaboration, R. Aaij *et al.*, “First Evidence for the Decay $B_s^0 \rightarrow \mu^+\mu^-$,” *Phys. Rev. Lett.* **110** no. 2, (2013) 021801, [arXiv:1211.2674 \[hep-ex\]](#).
- [61] **LHCb** Collaboration, R. Aaij *et al.*, “Observation of the resonant character of the $Z(4430)^-$ state,” *Phys. Rev. Lett.* **112** no. 22, (2014) 222002, [arXiv:1404.1903 \[hep-ex\]](#).
- [62] **LHCb** Collaboration, R. Aaij *et al.*, “Measurement of J/ψ production in pp collisions at $\sqrt{s} = 7$ TeV,” *Eur. Phys. J. C* **71** (2011) 1645, [arXiv:1103.0423 \[hep-ex\]](#).
- [63] **LHCb** Collaboration, R. Aaij *et al.*, “Determination of the X(3872) meson quantum numbers,” *Phys. Rev. Lett.* **110** (2013) 222001, [arXiv:1302.6269 \[hep-ex\]](#).
- [64] M. Su, T. R. Slatyer, and D. P. Finkbeiner, “Giant Gamma-ray Bubbles from Fermi-LAT: AGN Activity or Bipolar Galactic Wind?,” *Astrophys. J.* **724** (2010) 1044–1082, [arXiv:1005.5480 \[astro-ph.HE\]](#).
- [65] T. R. Slatyer, N. Padmanabhan, and D. P. Finkbeiner, “CMB Constraints on WIMP Annihilation: Energy Absorption During the Recombination Epoch,” *Phys. Rev. D* **80** (2009) 043526, [arXiv:0906.1197 \[astro-ph.CO\]](#).
- [66] D. Hooper and T. R. Slatyer, “Two Emission Mechanisms in the Fermi Bubbles: A Possible Signal of Annihilating Dark Matter,” *Phys. Dark Univ.* **2** (2013) 118–138, [arXiv:1302.6589 \[astro-ph.HE\]](#).
- [67] T. R. Slatyer, “Indirect dark matter signatures in the cosmic dark ages. I. Generalizing the bound on s-wave dark matter annihilation from Planck results,” *Phys. Rev. D* **93** no. 2, (2016) 023527, [arXiv:1506.03811 \[hep-ph\]](#).
- [68] S. K. Lee, M. Lisanti, B. R. Safdi, T. R. Slatyer, and W. Xue, “Evidence for Unresolved γ -Ray Point Sources in the Inner Galaxy,” *Phys. Rev. Lett.* **116** no. 5, (2016) 051103, [arXiv:1506.05124 \[astro-ph.HE\]](#).
- [69] G. Dobler, D. P. Finkbeiner, I. Cholis, T. R. Slatyer, and N. Weiner, “The Fermi Haze: A Gamma-Ray Counterpart to the Microwave Haze,” *Astrophys. J.* **717** (2010) 825–842, [arXiv:0910.4583 \[astro-ph.HE\]](#).
- [70] T. Cohen, M. Lisanti, A. Pierce, and T. R. Slatyer, “Wino Dark Matter Under Siege,” *JCAP* **10** (2013) 061, [arXiv:1307.4082 \[hep-ph\]](#).
- [71] M. S. Madhavacheril, N. Sehgal, and T. R. Slatyer, “Current Dark Matter Annihilation Constraints from CMB and Low-Redshift Data,” *Phys. Rev. D* **89** (2014) 103508, [arXiv:1310.3815 \[astro-ph.CO\]](#).

- [72] D. P. Finkbeiner, S. Galli, T. Lin, and T. R. Slatyer, “Searching for Dark Matter in the CMB: A Compact Parameterization of Energy Injection from New Physics,” *Phys. Rev. D* **85** (2012) 043522, [arXiv:1109.6322 \[astro-ph.CO\]](#).
- [73] M. Papucci, J. T. Ruderman, and A. Weiler, “Natural SUSY Endures,” *JHEP* **09** (2012) 035, [arXiv:1110.6926 \[hep-ph\]](#).
- [74] L. J. Hall, D. Pinner, and J. T. Ruderman, “A Natural SUSY Higgs Near 126 GeV,” *JHEP* **04** (2012) 131, [arXiv:1112.2703 \[hep-ph\]](#).
- [75] M. Freytsis, Z. Ligeti, and J. T. Ruderman, “Flavor models for $\bar{B} \rightarrow D^{(*)}\tau\bar{\nu}$,” *Phys. Rev. D* **92** no. 5, (2015) 054018, [arXiv:1506.08896 \[hep-ph\]](#).
- [76] A. Falkowski, J. T. Ruderman, and T. Volansky, “Asymmetric Dark Matter from Leptogenesis,” *JHEP* **05** (2011) 106, [arXiv:1101.4936 \[hep-ph\]](#).
- [77] C. Cheung, L. J. Hall, D. Pinner, and J. T. Ruderman, “Prospects and Blind Spots for Neutralino Dark Matter,” *JHEP* **05** (2013) 100, [arXiv:1211.4873 \[hep-ph\]](#).
- [78] A. Falkowski, J. T. Ruderman, T. Volansky, and J. Zupan, “Hidden Higgs Decaying to Lepton Jets,” *JHEP* **05** (2010) 077, [arXiv:1002.2952 \[hep-ph\]](#).
- [79] J. Fan, M. Reece, and J. T. Ruderman, “A Stealth Supersymmetry Sampler,” *JHEP* **07** (2012) 196, [arXiv:1201.4875 \[hep-ph\]](#).
- [80] J. Fan, A. Katz, L. Randall, and M. Reece, “Dark-Disk Universe,” *Phys. Rev. Lett.* **110** no. 21, (2013) 211302, [arXiv:1303.3271 \[hep-ph\]](#).
- [81] N. Arkani-Hamed, K. Blum, R. T. D’Agnolo, and J. Fan, “2:1 for Naturalness at the LHC?,” *JHEP* **01** (2013) 149, [arXiv:1207.4482 \[hep-ph\]](#).
- [82] K. Blum, R. T. D’Agnolo, and J. Fan, “Natural SUSY Predicts: Higgs Couplings,” *JHEP* **01** (2013) 057, [arXiv:1206.5303 \[hep-ph\]](#).